

NO CALCULATOR!! SHOW ALL WORK AND EXPRESS EACH ANSWER IN SIMPLEST FORM!

1. State the domain of each function *using interval notation*.

a) $f(x) = \sqrt{x+16}$ b) $p(x) = \sqrt{14-3x}$ c) $g(x) = \frac{\sqrt{8-x}}{x+7}$ d) $f(x) = \frac{2x+3}{\sqrt{5-x}}$ e) $g(x) = \frac{\sqrt{5-x}}{\sqrt{x+3}}$

2. Simplify:

a) $\frac{4}{4x}$ b) $\frac{5x}{\frac{1}{3}}$ c) $\frac{-2}{\frac{4}{x}}$ d) $\frac{x-3}{\frac{1}{x^2}}$

3. Let $f(x) = 2 - 6x$ and $g(x) = \frac{2}{3x}$

a) Find $\left(\frac{f}{g}\right)(x)$ b) Find $(f \circ g)(x)$ c) Find $(g \circ f)(x)$

4. Use the function $f(x) = 3x^2 - 5$ to evaluate the indicated expressions.

a) $f\left(\frac{2}{3}\right)$ b) $f(2)$ c) $f(2x)$ d) $2f(x)$

5. If $f(x) = 3x - 2$ and $g(x) = \frac{1}{6x^2}$, determine the following:

a) $(f \cdot g)(x)$ b) $(f \circ g)(x)$ c) $(g \circ f)(2)$

d) $\left(\frac{f}{g}\right)(x)$ e) $(f \circ f)(x)$

CHECK ANSWERS#1-3

$x \leq \frac{14}{3}$ therefore $\left(-\infty, \frac{14}{3}\right]$

$x \geq -16$ therefore $[-16, \infty)$

$x < 5$ therefore $(-\infty, 5)$

$-3 < x \leq 5$ therefore $(-3, 5]$

$x \neq -7$ and $x \leq 8$ therefore $(-\infty, -7) \cup (-7, 8]$

$3x - 9x^2$ $15x$ $x^3 - 3x^2$
 $-\frac{x}{2}$ $\frac{1}{x}$ $\frac{1}{3-9x}$ $2 - \frac{4}{x}$

CHECK ANSWERS#4-7

$f(x) = -2\sqrt{x+3} + 7$

$\frac{3x-2}{6x^2}$ $\frac{-11}{3}$ 7 $\frac{1}{96}$

$\frac{1}{2x^2} - 2$ $18x^3 - 12x^2$

$6x^2 - 10$ $9x - 8$ $12x^2 - 5$

$\frac{5x+7}{x-2}$ $\sqrt[3]{2-5x}$ $\frac{6x}{1-x}$

6. A function f is given and the indicated transformations are applied to its graph (in the given order.) Write the equation for the final transformed graph. $f(x) = \sqrt{x} \rightarrow$ stretch vertically by a factor of 2, reflect across the x -axis, shift 3 units to the left, and shift upward 7 units.

7. Find the inverse of the given functions.

a) $f(x) = \frac{2-x^3}{5}$

b) $g(x) = \frac{x}{x+6}$

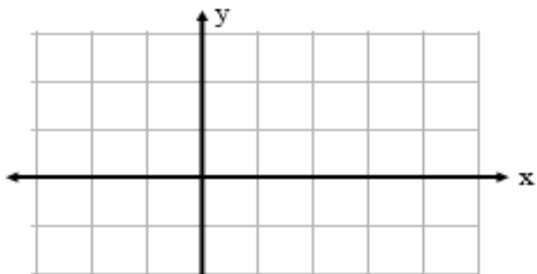
c) $h(x) = \frac{2x+7}{x-5}$

CHECK ANSWERS: -2 -1 -1 -1 0 0 2 2 3 $\pm i$ $\pm 2i$ $\pm\sqrt{3}$
 $y = 4(x + 3)^2 - 9$ $x^2 - 3x + 1$ $(x + 1)(x - 2)^3$ $x^2(x - 3)(x + 1)$ $(0, 27)$ $(3, 4)$ $(-3, -9)$
 $y = 5(x - 3)^2 + 4$ $x(x^2 + 4)(x^2 - 3)$ $(x + 2)(x - 2)(x^2 + 1)$ $\left(-\frac{9}{2}, 0\right)$ $\left(-\frac{3}{2}, 0\right)$

8. Given: $f(x) = 5x^2 - 30x + 49$
 Write the equation in standard form by completing the square, then identify the vertex.

9. Given: $f(x) = 4x^2 + 24x + 27$
 Write the equation in standard form by completing the square, then identify x- & y-intercepts and vertex.

10. Factor, then identify the zeros of $P(x)$ and sketch a graph. $P(x) = x^4 - 2x^3 - 3x^2$



11. Factor, then identify all real and complex zeros.
(Solve as is by factoring, no synthetic division.)

a) $P(x) = x^4 - 3x^2 - 4$

b) $R(x) = x^5 + x^3 - 12x$

12. Identify the **quotient** and the **remainder** using synthetic division:

$$(x^3 - 8x + 2) \div (x + 3)$$

13. Using synthetic division, **completely factor** $P(x)$ AND find all **zeros** of $P(x) = x^4 - 5x^3 + 6x^2 + 4x - 8$